Objective &	Concrete	Pictorial	Abstract
Strategy			
Adding multiples of	50= 30 = 20		20 + 30 = 50
ten			70 = 50 + 20
		3 tons + 5 tons = tens 30 + 50 =	40 + □ = 60
	Model using dienes and bead strings	Use representations for base ten.	
Use known number	Children ex-		+ 1 = 16 16 - 1 =
facts	plore ways of making num-	20	1 + = 16 16 = 1
Part part whole	bers within 20	+ = 20 20 - =	
	944	+ = 20 20 - =	
Using known facts	+ =	∵ + ÷ = ∴	3 + 4 = 7
	nnn <b>n</b> nn nnn <b>n</b> n	1(  +     =	leads to
			30 + 40 = 70
		• '•• ::•	leads to
		Children draw representations of H,T and O	300 + 400 = 700
Bar model		AAAAAAA A A A	23 25
		9999999 9 9 9	?
	3 + 4 = 7	7 + 3 = 10	23 + 25 = 48

Objective &	Concrete	Pictorial	Abstract
Strategy			
Add a two digit number and ones	17 + 5 = 22  Use ten frame to make 'magic ten  Children explore the pattern.  17 + 5 = 22  27 + 5 = 32	Use part part whole and number line to model.  17 + 5 = 22  3 2  16 + 7	17 + 5 = 22  Explore related facts  17 + 5 = 22  5 + 17 = 22  22-17 = 5  22-5 = 17
Add a 2 digit num- ber and tens	25 + 10 = 35 Explore that the ones digit does not change	27 + 30 +10 +10 +10 	27 + 10 = 37 27 + 20 = 47 27 + $\square$ = 57
Add two 2-digit numbers	Model using dienes , place value counters and numicon	+20 +5 Or +20 +3 +2  47 67 72 47 67 70 72  Use number line and bridge ten using part whole if necessary.	25 + 47 20 + 5 40 + 7 20 + 40 = 60 5+ 7 = 12 60 + 12 = 72
Add three 1-digit numbers	Combine to make 10 first if possible, or bridge 10 then add third digit	Regroup and draw representation.  + = 15	4+7+6 = 10+7  = 17  Combine the two numbers that make/ bridge ten then add on the third.

Objective & Strategy	Concrete	Pictorial	Abstract
Regroup a ten into ten ones	Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'	20 – 4 =	20—4 = 16
Partitioning to sub- tract without re- grouping. 'Friendly numbers'	Use Dienes to show how to partition the number when subtracting without regrouping.	Children draw representations of Dienes and cross off.	43—21 = 22
Make ten strategy  Progression should be crossing one ten, crossing more than one ten, crossing the hundreds.	34—28 Use a bead bar or bead strings to model counting to next ten and the rest.	76 80 90 93  'counting on' to find 'difference'  Use a number line to count on to next ten and then the rest.	93—76 = 17

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Objective &	Concrete	Pictorial	Abstract
Strategy			
Doubling	Model doubling using dienes and PV counters.  40 + 12 = 52	Draw pictures and representations to show how to double numbers	Partition a number and then double each part before recombining it back together.  16 10 10 1 12 20 1 x2 20 1 12 = 32
Counting in multi-	Count the groups as children are skip	Number lines, counting sticks and bar	Count in multiples of a number aloud.
ples of 2, 3, 4, 5, 10 from 0 (repeated addition)	counting, children may use their fingers as they are skip counting. Use bar models.  5+5+5+5+5+5+5+5+5=40	models should be used to show representation of counting in multiples.	Write sequences with multiples of numbers.  0, 2, 4, 6, 8, 10  0, 3, 6, 9, 12, 15  0, 5, 10, 15, 20, 25, 30

Objective &	Concrete	Pictorial	Abstract
Multiplication is commutative	Create arrays using counters and cubes and Numicon.  Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.	Use representations of arrays to show different calculations and explore commutativity.	12 = 3 × 4  12 = 4 × 3  Use an array to write multiplication sentences and reinforce repeated addition.  5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15
Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.		8   x   =	2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8 ÷ 2 Show all 8 related fact family sentences.

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Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities.  8 + 2 = 4  Children use bar modelling to show and support understanding.	12 ÷ 3 = 4
Division as grouping	Divide quantities into equal groups.  Use cubes, counters, objects or place value counters to aid understanding.	Use number lines for grouping  12 ÷ 3 = 4  Think of the par as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.  20  20  20  7	28 ÷ 7 = 4  Divide 28 into 7 groups. How many are in each group?